

## Lecture 2

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### 幅度调制 I

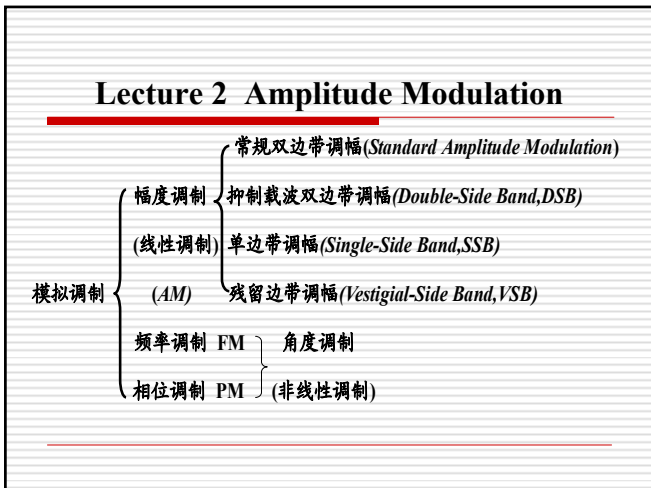
### Amplitude Modulation

## Lecture 2 Amplitude Modulation

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- **载波调制(Carrier Modulation):**  
将载波变换为一个载有信息的已调信号
- **解调(De-Modulation):**  
接收端从已调信号中恢复基带信号

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- ## Lecture 2 Amplitude Modulation
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- **常规双边带调幅(Standard AM)**
    - ◆ 时域表达
    - ◆ 调制过程
    - ◆ 频域表达
    - ◆ 解调过程
    - ◆ 功率分配
  - **双边带调幅(Double-Side Band, DSB)**
  - **单边带调幅(Single-Side Band, SSB)**
  - **残留边带调幅(Vestigial-Side Band, VSB)**
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## Standard AM的时域表示

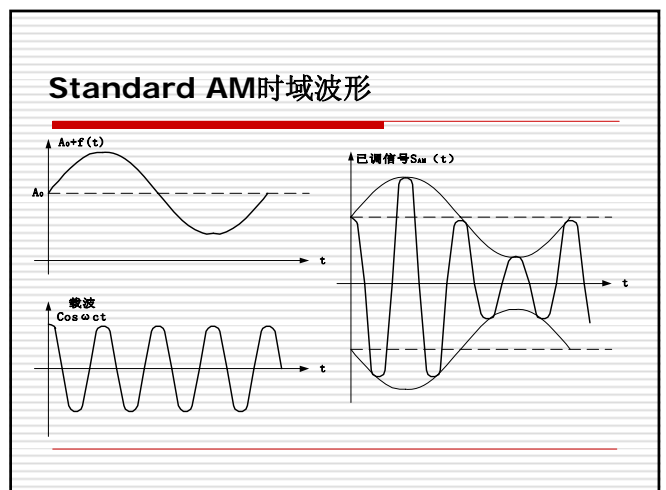
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- **幅度调制:**用基带信号 $f(t)$ 去迫使高频载波的瞬时幅度随 $f(t)$ 的变化而变化
- **Standard AM:**

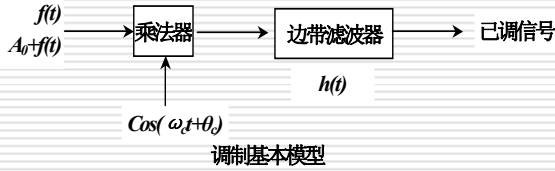
$$S_{AM}(t) = [A_0 + f(t)] \cos(\omega_c t + \theta_c)$$

其中  $\omega_c$  为载波角频率  
 $\theta_c$  为载波起始相位  
 $A_0$  为载波幅度

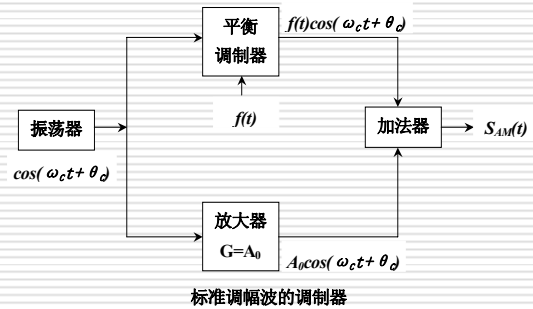
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### 标准调幅的调制过程



### 标准调幅的调制过程



### AM信号的频域表示

$$S_{AM}(t) = [A_0 + f(t)] \cos(\omega_c t + \theta_c)$$

$$= [A_0 + f(t)] \cdot \left[ \frac{e^{j(\omega_c t + \theta_c)} + e^{-j(\omega_c t + \theta_c)}}{2} \right]$$

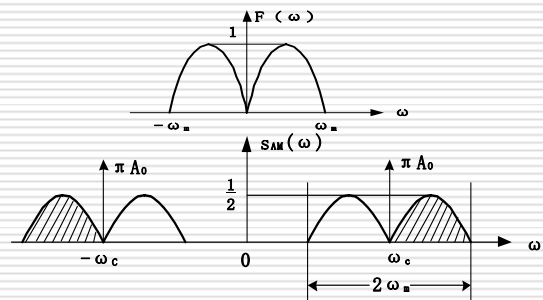
$$S_{AM}(\omega) = \left[ 2\pi A_0 \delta(\omega - \omega_c) + F(\omega - \omega_c) \right] \frac{e^{j\theta_c}}{2}$$

$$+ \left[ 2\pi A_0 \delta(\omega + \omega_c) + F(\omega + \omega_c) \right] \frac{e^{-j\theta_c}}{2}$$

令  $\theta_c = 0 \Rightarrow S_{AM}(\omega) = \pi A_0 \delta(\omega - \omega_c) + \frac{F(\omega - \omega_c)}{2}$

$$+ \pi A_0 \delta(\omega + \omega_c) + \frac{F(\omega + \omega_c)}{2}$$

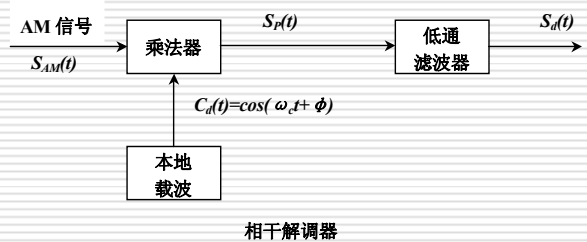
### AM信号的频域表示



### AM信号的频域表示

- 将  $F(\omega)$  搬移到载波频率(载频)  $f_c$  附近;
- $|\omega| \geq \omega_c$  上边带(USB);  
 $|\omega| \leq \omega_c$  下边带(LSB);
- 带宽  
 $B_{AM} = \frac{1}{2\pi} [(\omega_c + \omega_m) - (\omega_c - \omega_m)] = 2f_m = 2B$
- 两个冲激

### AM解调—相干解调



相位相干(Phase-coherent)/同步(Synchronous)

**相干解调：同步（相位差问题）**

乘法器的输入：

$$S_{AM}(t)=[A_0+f(t)]\cos(\omega_c t + \theta_c)$$

$$C_d(t)=\cos(\omega_c t + \phi)$$

乘法器的输出：

$$S_p(t)=S_{AM}(t)C_d(t)$$

$$=[A_0+f(t)]\cos(\omega_c t + \theta_c)\cos(\omega_c t + \phi)$$

$$=[A_0+f(t)][\cos(\theta_c - \phi) + \cos(2\omega_c t + \theta_c + \phi)]/2$$

用LPF滤除 $2\omega_c$ 的分量：

$$S_d(t)=[A_0+f(t)]\cos(\theta_c - \phi)/2$$

**相干解调：同步（频率差问题）**

本地载波

$$C_d(t)=\cos(\omega_c t + \Delta\omega t + \theta_c)$$

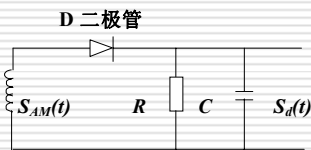
输出

$$S_d(t)=[A_0+f(t)]\cos\Delta\omega t/2$$

锁相环技术

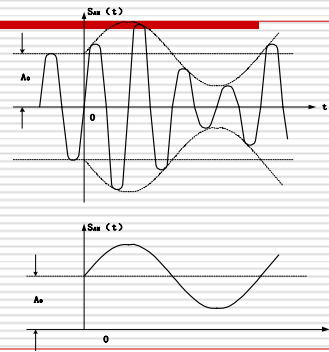
**AM解调--非相干解调**

**包络检波(Envelope Detection)**



$$S_d(t) \approx A_0 + f(t)$$

**AM解调--非相干解调**



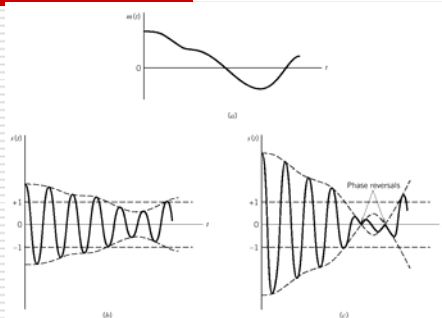
**AM解调--非相干解调**

为防止过调制的出现  
必须

$$A_0 + f(t) \geq 0$$

即

$$|f(t)|_{max} \leq A_0$$



**AM调制功率分配**

调制效率

AM信号的总平均功率为

$$P_s = \overline{S_{AM}^2(t)} = \overline{[A_0 + f(t)]^2 \cos^2 \omega_c t}$$

$$= A_0^2 \overline{\cos^2 \omega_c t} + \overline{f^2(t) \cos^2 \omega_c t} + 2 \overline{f(t) A_0 \cos^2 \omega_c t}$$

$f(t)$ 无直流分量

$$\therefore \overline{f(t)} = 0$$

$$\overline{\cos^2 \omega_c t} = \frac{1}{2} \overline{(1 + \cos 2\omega_c t)}, \quad \overline{\cos 2\omega_c t} = 0 \Rightarrow \overline{\cos^2 \omega_c t} = \frac{1}{2}$$

### AM调制功率分配

$$\therefore P_S = \frac{A_0^2}{2} + \frac{\overline{f^2(t)}}{2} = P_C + P_{SB}$$

$$\text{调制效率 } \eta_{AM} = \frac{P_{SB}}{P_{AM}} = \frac{P_{SB}}{P_{SB} + P_C} = \frac{\overline{f^2(t)}}{A_0^2 + \overline{f^2(t)}}$$

避免过调幅现象出现, 必须

$$|f(t)|_{max} \leq A_0$$

$$\therefore \eta_{AM} \leq 50\%$$

### AM调制功率分配

□ 正弦单频调制情况

$$f(t) = A_m \cos \Omega t$$

$$S_{AM}(t) = [A_0 + A_m \cos \Omega t] \cos(\omega_c t + \theta_c) \\ = A_0 [1 + \beta_{AM} \cos \Omega t] \cos(\omega_c t + \theta_c)$$

□ 调幅指数

$$\beta_{AM} = \frac{|f(t)|_{max}}{A_0} = \frac{A_m}{A_0}$$

□ 为防止过调制, 要求

$$\beta_{AM} \leq 1$$

### AM调制功率分配

$$S_{AM}(t) = A_0 \cos(\omega_c t + \theta_c) + \frac{1}{2} \beta_{AM} A_0 \cos[(\omega_c - \Omega)t + \theta_c]$$

$$+ \frac{1}{2} \beta_{AM} A_0 \cos[(\omega_c + \Omega)t + \theta_c]$$

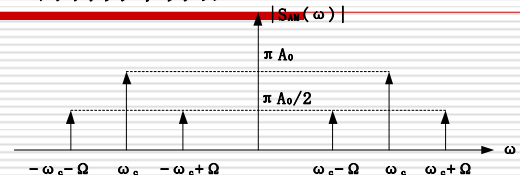
令  $\theta_c = 0$

$$S_{AM}(\omega) = \pi A_0 [\delta(\omega - \omega_c) + \delta(\omega + \omega_c)]$$

$$+ \frac{\pi A_0}{2} [\delta(\omega - \omega_c - \Omega) + \delta(\omega - \omega_c + \Omega)]$$

$$+ \frac{\pi A_0}{2} [\delta(\omega + \omega_c - \Omega) + \delta(\omega + \omega_c + \Omega)]$$

### AM调制功率分配



$$\eta_{AM} = \frac{\overline{f^2(t)}}{A_0^2 + \overline{f^2(t)}} = \frac{\frac{1}{2} A_m^2}{A_0^2 + \frac{1}{2} A_m^2} = \frac{\beta_{AM}^2}{2 + \beta_{AM}^2}$$

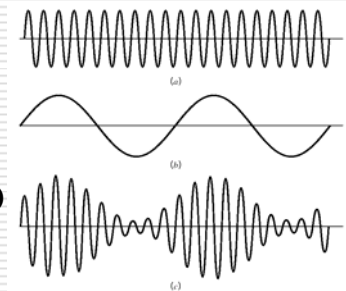
临界状态下  $\beta_{AM} = 1$  ( $\eta_{AM})_{max} = 1/3$

### Lecture 2 Amplitude Modulation

- 常规双边带调幅(Standard Amplitude Modulation)
- 抑制载波双边带调幅(Double-Side Band, DSB)
- 单边带调幅(Single-Side Band, SSB)
- 残留边带调幅(Vestigial-Side Band, VSB)

### DSB-AM的时域表示

$$S_{DSB}(t) = f(t) \cos(\omega_c t + \theta_c)$$



### DSB-AM的频域表示

$$S_{DSB}(\omega) = \frac{1}{2}F(\omega - \omega_c)e^{j\theta_c} + \frac{1}{2}F(\omega + \omega_c)e^{-j\theta_c}$$

令  $\theta_c = 0$

$$= \frac{1}{2}F(\omega - \omega_c) + \frac{1}{2}F(\omega + \omega_c)$$

### DSB-AM的频域表示

□ 线性搬移

□ USB/LSB

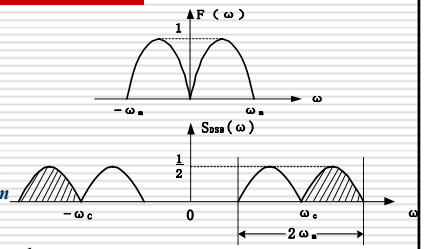
□ 带宽

$$B_{DSB} = 2B = 2f_m$$

□ 调制效率

$$P_{DSB} = S_{DSB}^2(t) = \frac{1}{2}f^2(t) = P_{SB}$$

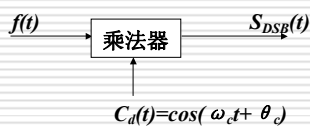
$$\eta = 100\%$$



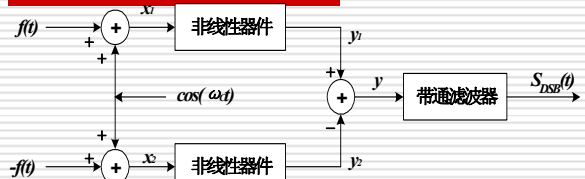
### DSB-AM的调制

□  $S_{DSB}(t) = f(t)\cos(\omega_c t + \theta_c)$

□ 乘法器—平衡调制器(Balanced Modulator)



### DSB-AM的调制



例：若非线性器件的输入-输出特性为： $y = a_1x + a_2x^2$

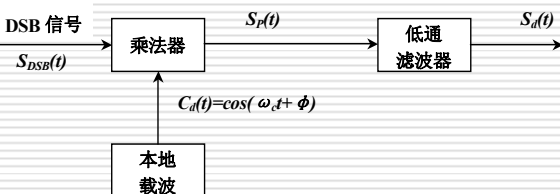
解：由图  $x_1 = f(t) + \cos \omega_c t$  ;  $x_2 = -f(t) + \cos \omega_c t$

$$y_1 = a_1[f(t) + \cos \omega_c t] + a_2[f(t) + \cos \omega_c t]^2$$

$$y_2 = a_1[-f(t) + \cos \omega_c t] + a_2[-f(t) + \cos \omega_c t]^2$$

$$\therefore y = y_1 - y_2 = 2a_1f(t) + 4a_2f(t)\cos \omega_c t \rightarrow \text{BPF}$$

### DSB的解调--相干解调



相干解调器

$$S_d(t) = f(t)\cos(\theta_c - \phi)/2$$